

## TL;DR

- (i) We show that KL-regularized RL with behavioral reference policies derived from expert demonstrations can suffer from pathological training dynamics caused by a collapse in the predictive variance of behavioral reference policies about states away from the expert demonstrations.
- (ii) We demonstrate that this pathology can lead to instability and suboptimality in online learning, but that it can be prevented by specifying non-parametric behavioral reference policies whose predictive variance is guaranteed not to collapse about previously unseen states.
- (iii) We show that fixing the pathology allows KL-regularized RL to significantly outperform state-of-the-art approaches on a range of challenging locomotion and dexterous manipulation tasks.



**Figure 1:** Dexterous hand manipulation tasks on which our fix leads to a significant acceleration in training and improvement in performance.

### Reinforcement Learning & Behavioral Cloning

- •An agent interacts with a discounted Markov Decision Process  $(\mathcal{S}, \mathcal{A}, p, r, \gamma)$ .  $\mathcal{S}$  and  $\mathcal{A}$  are the state and action spaces,  $p(\cdot | \mathbf{s}_t, \mathbf{a}_t)$  are the transition dynamics,  $r(\mathbf{s}_t, \mathbf{a}_t)$  is the reward function, and  $\gamma$  is a discount factor. The agent learns a policy  $\pi(\mathbf{a} \mid \mathbf{s})$ .
- In behavioral cloning, a mapping  $\pi_0 : S \to A$  is learned from an offline dataset  $\mathcal{D}_0 = \{(\bar{\mathbf{s}}_i, \bar{\mathbf{a}}_i)\}_{i=1}^n$  of expert demonstrations, with n typically in the order of 1k - 10k.

# ON PATHOLOGIES IN KL-REGULARIZED REINFORCEMENT LEARNING FROM EXPERT DEMONSTRATIONS

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# Identifying the Pathology

### **KL-Regularized Reinforcement Learning**

the reward with a KL-penalty:

$$\sum_{t=0}^{\infty} \mathbb{E}_{(\mathbf{s}_t, \mathbf{a}_t) \sim \rho_{\pi}} \left[ \gamma^t \left( r(\mathbf{s}_t, \mathbf{a}_t) \right) \right]$$

- with in the support of  $\pi_0$ .
- data manifold, effectively leading to a loss in support between  $\pi$  and  $\pi_0$ .



Figure 2: Predictive variances of non-parametric and parametric behavioral policies on a low dimensional representation of a 39-dimensional dexterous hand manipulation state space (doorbinary-v0). Left: Non-parametric Gaussian process posterior behavioral policy  $\pi_{\mathcal{GP}}(\cdot | \mathbf{s}, \mathcal{D}_0) = \mathbf{s}$  $\mathcal{GP}(\mu_0(\mathbf{s}), \Sigma_0(\mathbf{s}, \mathbf{s}'))$ . **Right**: Parametric neural network Gaussian behavioral policy  $\pi_{\psi}(\cdot | \mathbf{s}) = 1$  $\mathcal{N}(\boldsymbol{\mu}_{\psi}(\mathbf{s}), \boldsymbol{\sigma}_{\psi}(\mathbf{s}))$ . Expert trajectories  $\mathcal{D}$  used to train the behavioral policies are shown in black.

0, when  $\nabla_{\phi} f_{\phi}(\epsilon_t; \mathbf{s}_t) \neq 0$ .

**Full paper**: timrudner.com/rl-pathologies

• Given a reference policy  $\pi_0$  and temperature  $\alpha$ , KL-regularized RL augments

$$\alpha \mathbb{D}_{\mathrm{KL}}(\pi(\cdot \mid \mathbf{s}_t) \mid \mid \pi_0(\cdot \mid \mathbf{s}_t))) \Big]$$

• For the KL divergence to be defined, we require the support of  $\pi$  to be contained

• Behaviorally cloned stochastic policies parameterized by a neural network via MLE experience a collapse in predictive variance about states off the offline

**Proposition 1** (Exploding Gradients in KL-Regularized RL; ). Let  $\pi_0(\cdot | \mathbf{s})$  be a Gaussian behavioral policy with mean  $\mu_0(\mathbf{s}_t)$  and variance  $\sigma_0^2(\mathbf{s}_t)$ , and let  $\pi_{\phi}(\cdot \,|\, \mathbf{s})$ be an online policy with reparameterization  $\mathbf{a}_t = f_{\phi}(\epsilon_t; \mathbf{s}_t)$  and random vector  $\epsilon_t$ . Let the gradient of the policy loss with respect to the online policy's parameters  $\phi$  be denoted  $\nabla_{\phi} J_{\pi}(\phi)$ . For fixed  $|\mathbf{a}_t - \boldsymbol{\mu}_0|$ ,  $|\nabla_{\phi} J_{\pi}(\phi)| \to \infty$  as  $\sigma_0^2 \to \sigma_0^2$ 









HalfCheetah-v2 environment using different behavioral policies.